



















Least Positive Solution to the Balance Equations

Note that if p_C , c_C , the number of tokens produced and consumed on a connection C, are non-negative integers, then the balance equation,

$$q_A p_C = q_B c_C$$

implies:

- q_A is rational if an only if q_B is rational.
- q_A is positive if an only if q_B is positive.

Consequence: Within any connected component, if there is any solution to the balance equations, then there is a unique least positive integer solution.

EECS 124, UC Berkeley: 11

Rank of a Matrix The rank of a matrix Γ is the number of linearly independent rows or columns. The equation $\Gamma q = \vec{0}$ is forming a linear combination of the columns of G. Such a linear combination can only yield the zero vector if the columns are linearly dependent (this is what is means to be linearly dependent). If Γ has *a* rows and *b* columns, the rank cannot exceed min(*a*, *b*). If the columns or rows of Γ are re-ordered, the resulting matrix has the same rank as Γ . EECS 124, UC Berkeley: 12





















