Overview

Introduction to Safe State Machines and Esterel
  Signals and Synchrony
  The ABRO Example
  Write Things Once
  The multiform notion of time
  Uses, Advantages, Disadvantages

Esterel Language Overview

Esterel/SSM Pragmatics

Interfacing with the Environment
Introduction to Esterel

- Imperative, textual, concurrent language
- Developed since early 1980s (Gérard Berry)
- Based on synchronous model of time
  - Program execution synchronized to an external clock
  - Like synchronous digital logic
  - Suits the cyclic executive approach
- Same *model of computation* as SyncCharts/Safe State Machines (SSMs)
- EsterelStudio generates Esterel from SSMs as intermediate code
- Currently undergoing IEEE standardization (Esterel v7)

*Thanks to Stephen Edwards (http://www1.cs.columbia.edu/~sedwards/) for providing part of the following material*
Introduction to Esterel

Time is divided into discrete ticks (also called cycles, steps, instants)

Two types of statements:
- Those that take “zero time” (execute and terminate in same tick, e.g., emit)
  - Correspond to Connectors in SSMs
- Those that delay for a prescribed number of ticks (e.g., await)
  - Correspond to States in SSMs
Signals

- Esterel programs/SSMs communicate through **signals**
- These are like wires
  - Each signal is either **present** or **absent** in each tick
  - Can’t take multiple values within a tick
- Presence/absence not held between ticks
- Broadcast across the program
  - Any process can read or write a signal
Signals

- Status of an input signal is determined by input event, and by local emissions
- Status of local or output signal is determined per tick
  - Default status: absent
  - Must execute an “emit S” statement to set signal S present
- await A:
  - Waits for A and terminates when A occurs
Synchrony Hypothesis

- Computations are considered to
  - take no time
  - be atomic

G. Luettgen 2001
Synchronous Model of Computation

To summarize: the synchronous model of computation of SSMs/Esterel is characterized by:

1. Computations considered to take no time (synchrony hypothesis)
2. Time is divided into discrete ticks
3. Signals are either present or absent in each tick

Sometimes, “synchrony” refers to just the first two points (e.g., in the original Statecharts as implemented in Statemate); to explicitly include the third requirement as well, we also speak of the strict synchrony.
Consider the following controller specification:

- Emit the output 0 as soon as both the inputs A and B have been received.
- Reset the behavior whenever the input R is received.

This is still a bit ambiguous; to complete:

- If R occurs, emit nothing
- Do nothing at initialization time
- Input signals may be simultaneous
The ABRO Example—Mealy Style
Write Things Once

- The disadvantage of this (flat) notation:
  - Size grows exponentially
  - A little change to the specification may incur a major change to the automaton (often ends with full rewriting)

- The answer:
  - Add hierarchy
  - More generally: Write Things Once (WTO)

- Analogy from language theory:
  - Use regular expressions to represent large (possibly infinite) sets of strings
ABRO—Safe State Machine
ABRO—The Esterel Version

module ABRO:
input A, B, R;
output O;

loop
  [ await A || await B ];
  emit O each R
end module

► Esterel programs built from modules
► Each module has an interface of input and output signals
► Much simpler since language includes notions of signals, waiting, and reset
ABRO—The Esterel Version

module ABRO:
  input A, B, R;
  output O;

loop
  [ await A || await B ];
  emit O
each R
end module

- loop ... each statement implements reset
- || runs the two awaits in parallel
- await waits for the next tick where its signal is present
- Parallel terminates when all its threads have
- emit 0 makes signal 0 present when it runs
The Multiform Notion of Time

- A design goal of synchronous languages:
  - Fully deterministic behavior
  - Applies to functionality and (logical) timing
- Approach:
  - Replace notion of physical time with notion of order
  - Only consider simultaneity and precedence of events
- Hence, physical time does not play any special role
  - Is handled like any other event from program environment
  - This is called multiform notion of time
Consider following requirements:

- “The train must stop within 10 seconds”
- “The train must stop within 100 meters”

These are conceptually of the same nature!

In languages where physical time plays particular role, these requirements are typically expressed completely differently.

In synchronous model, use similar precedence constraints:

- “The event stop must precede the 10th (respectively, 100th) next occurrence of the event second (respectively, meter)”
The Multiform Notion of Time

- **History** of system is a totally ordered sequence of logical ticks.
- At each tick, an arbitrary number of events (including 0) occurs.
- Event occurrences that happen at the same logical tick are considered **simultaneous**.
- Other events are **ordered** as their instances of occurrences.
Uses of SSMs/Esterel

- Wristwatch
  - Canonical example
  - Reactive, synchronous, hard real-time
- Controllers
  - Communication protocols
- Avionics
  - Fuel control system
  - Landing gear controller
  - Other user interface tasks
- Processor components (cache controller, etc.)
- General hw design
Advantages of SSMs/Esterel

- Model of time gives programmer precise control
- Concurrency convenient for specifying control systems
- Completely deterministic
  - Guaranteed: no need for locks, semaphores, etc.
- Finite-state language
  - Easy to analyze
  - Execution time predictable
  - Much easier to verify formally
- Amenable to implementation in both hardware and software
Disadvantages of SSMs/Esterel

- Finite-state nature of the language limits flexibility
  - No dynamic memory allocation
  - No dynamic creation of processes
- Virtually nonexistent support for handling data (this changes in v7)
  - Must resort to some host language (e.g., C) for that
- Really suited for simple decision-dominated controllers
- Synchronous model of time can lead to overspecification
- Semantic challenges
  - Avoiding causality violations often difficult
  - Difficult to compile
- Limited number of users, tools, etc.
Overview

Introduction to Safe State Machines and Esterel

Esterel Language Overview
  Signal emission + testing, pausing
  Esterel’s model of time
  Parallelism
  Signal awaiting, looping
  Preemption, exceptions, suspension

Esterel/SSM Pragmatics

Interfacing with the Environment
Basic Esterel Statements

**emit S**
- Make signal S present in the current instant
- A signal is absent unless it is emitted

**pause**
- Stop and resume after the next cycle after the pause

**present S then stmt1 else stmt2 end**
- If signal S is present in the current instant, immediately run `stmt1`, otherwise run `stmt2`
Esterel’s Model of Time

- The standard CS model (e.g., Java’s) is asynchronous
  - Threads run at their own rate
  - Synchronization is done (for example) through calls to `wait()` and `notify()`

- Esterel’s model of time is synchronous like that used in hardware. Threads march in lockstep to a global clock.
Basic Esterel Statements

```esterel
module EXAMPLE1:
    output A, B, C;

    emit A;
    present A then
        emit B
    end;
    pause;
    emit C

end module
```

EXAMPLE1 makes signals A & B present the first instant, C present the second
Transformation of EXAMPLE1 into SSMs

Structural translation of Esterel into SSMs

Performed with KIEL tool, www.informatik.uni-kiel.de/rtsys/kiel/
Transformation of EXAMPLE1 into SSMs

After some optimizations
Transformation of EXAMPLE1 into SSMs

Final version
Signal Coherence Rules

- Each signal is only present or absent in a cycle, never both.
- All writers run before any readers do.
- Thus

```plaintext
present A else
  emit A
end
```

is an erroneous program.
Advantage of Synchrony

- Easy to control time
- Synchronization comes for free
- Speed of actual computation nearly uncontrollable—Synchrony allows to specify function and timing independently
- Makes for deterministic concurrency
- Explicit control of “before” “after” “at the same time”
Time Can Be Controlled Precisely

This guarantees every 60th S an M is emitted:

\[
\text{every } 60 \text{ S do}
\]
\[
\text{emit } M
\]
\[
\text{end}
\]

\text{every invokes its body every 60th S}
\text{emit takes no time (cycles)}

\[
\begin{array}{cccccccc}
  S & S & S & S & S & S & S \\
  & M & & & & & M \\
  1 & \cdots & 59 & 60 & 61 & \cdots & 120
\end{array}
\]
The || Operator

Groups of statements separated by || run concurrently and terminate when all groups have terminated.

```
[  
  emit A;  
  pause; emit B;  
||  
  pause; emit C;  
  pause; emit D  
];  
emit E
```

A     B
C     D
     E
Communication Is Instantaneous

A signal emitted in a cycle is visible immediately

```
[   pause; emit A;
    pause; emit A
|
    pause;
    present A then
      emit B end
]```

Bidirectional Communication

Processes can communicate back and forth in the same cycle

\[
\begin{array}{l}
\text{[}
\text{pause; emit A;}
\text{present B then}
\text{emit C end;}
\text{pause; emit A}
\text{]}
\\
\text{||}
\text{pause;}
\text{present A then}
\text{emit B end}
\end{array}
\]
Concurrencey and Determinism

- Signals are the only way for concurrent processes to communicate
- Esterel does have variables, but they cannot be shared
- **Signal coherence rules ensure deterministic behavior**
- Language semantics clearly defines who must communicate with whom when
The Await Statement

- The `await` statement waits for a particular cycle.
- `await S` waits for the next cycle in which `S` is present.

```
[ emit A;
 pause;
 pause; emit A
] ||
 await A; emit B
```

Diagram:
```
A  A
---
     B
```
The Await Statement

- `await` normally waits for a cycle before beginning to check
- `await immediate` also checks the initial cycle

```plaintext
[  
etit A;
  pause;
  pause; emit A  
]|  
\await immediate A;
  emit B ]
```

A  
A   
B  

Fall 2007  
EE 249
Loops

- Esterel has an infinite loop statement
- **Rule:** loop body cannot terminate instantly
  - Needs at least one `pause`, `await`, etc.
  - Can't do an infinite amount of work in a single cycle

```plaintext
loop
  emit A;
  pause;
  pause;
  emit B
end
```

---

<table>
<thead>
<tr>
<th></th>
<th>A</th>
<th>A</th>
<th>A</th>
<th>A</th>
<th>A</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>B</td>
<td>B</td>
<td>B</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

---
Loops and Synchronization

Instantaneous nature of loops plus await provide very powerful synchronization mechanisms

```
loop
    await 60 S;
    emit M
end
```
Preemption

- Often want to stop doing something and start doing something else
- E.g., Ctrl-C in Unix: stop the currently-running program
- Esterel has many constructs for handling preemption
The Abort Statement

- Basic preemption mechanism
- General form:

\[
\text{abort} \\
\quad \text{statement} \\
\text{when} \quad \text{condition}
\]

- Runs \textit{statement} to completion
- If \textit{condition} ever holds, \textit{abort} terminates immediately.
The Abort Statement

```plaintext
abort
    pause;
    pause;
    emit A
when B;
emit C
```

- **Normal Termination**
  - A
    - C
  - B
  - C

- **Aborted termination**
  - B
  - C

- **Aborted termination; emit A preempted**
  - B
  - A
  - C

- **Normal Termination**
  - B not checked in first cycle (like await)
Strong vs. Weak Preemption

- **Strong preemption:**
  - The body does not run when the preemption condition holds
  - The previous example illustrated strong preemption

- **Weak preemption:**
  - The body is allowed to run even when the preemption condition holds, but is terminated thereafter
  - `weak abort` implements this in Esterel
Strong vs. Weak Abort

**Strong Abort**
- `abort`;
- `pause`;
- `pause`;
- `emit A`;
- `pause`;
- `when B`;
- `emit C`

**Weak Abort**
- `weak abort`;
- `pause`;
- `pause`;
- `emit A`;
- `pause`;
- `when B`;
- `emit C`

**Diagram**
- Emit A not allowed to run
- Emit A does run, body terminated afterwards
Strong vs. Weak Preemption

- Important distinction
- Something cannot cause its own strong preemption

```
abort
  pause;
  emit A
when A
```
Erroneous!

```
weak abort
  pause;
  emit A
when A
```
Ok!
Nested Preemption

module RUNNER
input SECOND, METER, LAP;
output ... ;

every MORNING do
  abort
  loop
    abort RUNSLOWLY when 15 SECOND;
    abort
    every STEP do
      JUMP || BREATHE
    end every
    when 100 METER;
    FULLSPEED
  each LAP
  when 2 LAP
end every
end module
 Exceptions—The Trap Statement

- Esterel provides an exception facility for *weak* preemption
- Interacts nicely with concurrency
- **Rule:** outermost trap takes precedence
The Trap Statement

```
trap T in
[
    pause;
    emit A;
    pause;
    exit T
]
||
    await B;
    emit C
]
end trap;
emit D
```

---

Normal termination from first process

- A \[\rightarrow\] D

emit C also runs

- A \[\rightarrow\] B
- C \[\rightarrow\] D

Second process allowed to run even though first process has exited

- A \[\rightarrow\] B
- C \[\rightarrow\] D
Nested Traps

```plaintext
trap T1 in
  trap T2 in
  [ exit T1
     ||
     exit T2
  ]
end;
emit A
end;
emit B
```

- Outer trap takes precedence; control transferred directly to the outer trap statement.
- `emit A` not allowed to run.
Combining Abortion and Exceptions

```plaintext
trap HEARTATTACK in
  abort
  loop
    abort RUNSLOWLY when 15 SECOND;
    abort
    every STEP do
      JUMP || BREATHE || CHECKHEART
    end every
    when 100 METER;
    FULLSPEED
    each LAP
    when 2 LAP
  handle HEARTATTACK do
    GOTOHOSPITAL
  end trap
```
The Suspend Statement

- Preemption (abort, trap) terminate something, but what if you want to pause it?
- Like the POSIX Ctrl-Z
- Esterel’s suspend statement pauses the execution of a group of statements
- Only strong preemption: statement does not run when condition holds
The Suspend Statement

```plaintext
suspend
  loop
    emit A;
    pause;
    pause
  end
when B
```

- **B delays emission of A by one cycle.**
- **B prevents A from being emitted here; resumed next cycle.**
Overview

Introduction to Safe State Machines and Esterel

Esterel Language Overview

Esterel/SSM Pragmatics
  People Counter Example
  Vending Machine Example
  Tail Lights Example
  Traffic-Light Controller Example

Interfacing with the Environment

Property Verification
People Counter Example

Construct an Esterel program that counts the number of people in a room.

- People enter the room from one door with a photocell that changes from 0 to 1 when the light is interrupted, and leave from a second door with a similar photocell. These inputs may be “1” for more than one clock cycle. It is assumed that one continuous sequence of 1’s corresponds to a single person passing the photocell. The two photocell inputs are called ENTER and LEAVE.

- There are two outputs: EMPTY and FULL, which are present when the room is empty and contains three people respectively.

Vending Machine Example

Design a vending machine controller that dispenses gum once.

- Two inputs, \( N \) and \( D \), are present when a nickel and dime have been inserted.

\[
N = \quad D =
\]

- A single output, \( \text{GUM} \), should be present for a single cycle when the machine has been given fifteen cents.

\[
\text{GUM} =
\]

- No change is returned.

Tail Lights Example

Construct an Esterel program that controls the turn signals of a 1965 Ford Thunderbird.

Tail Light Behavior
Tail Lights

- There are three inputs, which initiate the sequences: **LEFT**, **RIGHT**, and **HAZ**
- The flashing sequence is:

<table>
<thead>
<tr>
<th>LC</th>
<th>LB</th>
<th>LA</th>
<th>Step</th>
<th>RA</th>
<th>RB</th>
<th>RC</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>4</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

  [Diagram showing the flashing sequence with numbers 1 to 4 and states for each output.]
Traffic-Light Controller Example

Control a traffic light at the intersection of a busy highway and a farm road.


- Normally, the highway light is green
- If a sensor detects a car on the farm road:
  - The highway light turns yellow then red.
  - The farm road light then turns green until there are no cars or after a long timeout.
  - Then, the farm road light turns yellow then red, and the highway light returns to green.
- Inputs: The car sensor $C$, a short timeout signal $S$, and a long timeout signal $L$.
- Outputs: A timer start signal $R$, and the colors of the highway and farm road lights $HG$, $HY$, $HR$, $FG$, $FY$, and $FR$. 
Overview

Introduction to Safe State Machines and Esterel

Esterel Language Overview

Esterel/SSM Pragmatics

Interfacing with the Environment

Esterel Signal Types
  Option 1: Single pure signal
  Option 2: Two pure signals
  Option 3: Boolean valued signal

Property Verification
Interfacing with the Environment

- At some point, our reactive system must control real-world entities
- There are usually different options for the interface—differing in
  - Ease of use
  - Ease of making mistakes!
- **Example:** External device that can be ON or OFF
- **Options:**
  1. Single pure signal
  2. Two pure signals
  3. Boolean valued signal
Valued Signals

- Beside the status present or absent, a signal can have an additional value.
- Valued signals are declared with a certain type
- output $S$: integer declares an output signal of type integer
- emit $S(15)$ makes signal $S$ present and assigns it the value 15
- Value of signal $S$ can be tested by $?S$
- The value is persistent across logical ticks
- To preserve determinism, only one signal value per tick allowed
Valued Signals

Single valued signal:
- Only one statement can emit signal per instant

Combined valued signal:
- Multiple emitters allowed
- Indicated with `combine` keyword
- Are combined with (commutative and associative) binary operator
  - `boolean`: combination function can be `and` or `or`
  - `integer, float, double`: can use `+` or `*`
Variables

- ...are assignable objects with name and type
- ...similar rules as for signals (regarding placement, scoping)
- Value is undefined until first assignment

```plaintext
var
  X : double,
  Count := ? Distance : integer,
  Deadline : Time
in
  p
end var
```

- Must declare type individually for each variable
  - var X, Y integer is incorrect!
Different Modes of Motor Control

Option 1: Single pure signal

▶ Motor is running in every instant which has the **MOTOR** signal present

**Pro:**

▶ Minimal number of signals

**Con:**

▶ High number of signal emissions (signal is emitted in every instant where the motor is on)—may be unnecessary run-time overhead

▶ Somewhat heavy/unintuitive representation

```plaintext
input BUMPER;
output MOTOR;
abort sustain MOTOR
when BUMPER
```
Different Modes of Motor Control

Option 2: Two pure signals

- Motor is switched on with signal `MOTOR_ON` present
- Motor is switched off with signal `MOTOR_OFF` present
- If neither `MOTOR_ON` or `MOTOR_OFF` is present, motor keeps its previous state

Pro:

- Signal emissions truly indicate significant change of external state
- Simple representation in Esterel

Con:

- No way to control inconsistent outputs
- No memory - cannot check in retrospect which signal was emitted
Inconsistent Outputs

- Problem with MOTOR_ON and MOTOR_OFF: undefined behavior with both signals present
- Can address this at host-language level
- Can (and should) also address this at Esterel-level:

```esterel
present BUMPER else
  emit MOTOR_ON;
  await BUMPER
end present;
emit MOTOR_OFF
||
await immediate MOTOR_ON and MOTOR_OFF;
exit INTERNAL_ERROR
```
Valued Signal for Motor Control

Option 3: Boolean valued signal

- Merge pure signals MOTOR_ON and MOTOR_OFF into one valued signal MOTOR

- Motor is switched on if every emit-statement in that instant emits true

- Here: In case of conflicting outputs, motor stays switched off

```plaintext
input BUMPER;
output MOTOR
    combine BOOLEAN
    with and;
emit MOTOR(true);
await immediate BUMPER;
emit MOTOR(false);
```
Valued Signal for Motor Control

Option 3 contd.

Pro:

- Again only one signal for motor control
- Explicit control of behavior for inconsistent outputs
- Valued signal has memory—can be polled in later instances, after emission
- Easy extension to finer speed control

Con:

- Inconsistent outputs are handled deterministically—but are not any more detected and made explicit
- For certain classes of analyses/formal methods that we may wish to apply, valued signals are more difficult to handle than pure signals
Events vs. State

▶ Excessive signal emissions
  ▶ make the behavior difficult to understand
  ▶ cause overhead if fed to the external environment

▶ State:
  ▶ “Robot is turning left”
  ▶ “Motor is on”
  ▶ Esterel:
    ▶ waiting for some signal
    ▶ terminated thread
    ▶ value of valued signal

▶ Event:
  ▶ Change of State
  ▶ “Turn motor on”
  ▶ Esterel:
    ▶ emit pure signal
    ▶ change value of signal
Overview

Introduction to Safe State Machines and Esterel

Esterel Language Overview

Esterel/SSM Pragmatics

Interfacing with the Environment

Property Verification

Introduction

Example: ABRO
Property Verification

- One advantage of formal foundation of synchronous model: Ability to formally verify certain properties
- Can conveniently specify properties using observers, using the familiar SSM/Esterel formalism
- Observers scan for
  - Always type properties (must always be fulfilled)
  - Never type properties (should never occur)
- Verifier, based on model checking, is included in Esterel Studio
Example: ABRO

Property P1:

"O cannot be emitted if B has not been received since the last occurrence of R"

Observer for P1:
Screenshot of Esterel-Studio Verifier
Example: ABRO

Property P2:
O is never emitted twice since the last occurrence of R

Observer for P2:
Summary I

- Classical real-time languages include specific notions of physical time—however, they do not achieve complete determinism this way.
- Synchronous languages replace notion of physical time with notion of order, considering only simultaneity and precedence of events—this is the multiform notion of time.
- The Write-Things-Once principle aids to make representations compact, and to ease modifications. For state machines, WTO is achieved by adding hierarchy.
Summary II

- Esterel is an imperative, control-oriented synchronous language
- Synchronous model of time, as used by SSMs
  - Time divided into sequence of discrete ticks
  - Instructions either run and terminate in the same tick or explicitly in later ticks
- Idea of signals and broadcast
  - “Variables” that take exactly one value each tick and don’t persist
  - Coherence rule: all writers run before any readers
Summary III

- Esterel and SSMs are high-level descriptions—however, there are still several options to express the same behavior.
- May e.g. alternatively use state encoding or variable encoding to memorize control state across logical ticks.
- Can use macro facility to modularize description.
- Care should be taken to select a suitable interface with the environment—single pure signals, two pure signals, or Boolean valued signal.
- The formally founded semantics of Esterel allows to perform formal verification (for more, should attend additional class, e.g. “Verification of Concurrent Programs”.)
To Go Further


