

















Notation Velocity $\dot{\mathbf{x}}: \mathbb{R} \to \mathbb{R}^3$ is the derivative, $\forall t \in \mathbb{R}$, $\dot{\mathbf{x}}(t) = \frac{d}{dt}\mathbf{x}(t)$ Acceleration $\ddot{\mathbf{x}}: \mathbb{R} \to \mathbb{R}^3$ is the second derivative, $\ddot{\mathbf{x}} = \frac{d^2}{dt^2}\mathbf{x}$ Force on an object is $\mathbf{F}: \mathbb{R} \to \mathbb{R}^3$.

Newton's Second Law

Newton's second law states $\forall t \in \mathbb{R}$,

 $\mathbf{F}(t) = M\ddot{\mathbf{x}}(t)$

where M is the mass. To account for initial position and velocity, convert this to an <u>integral equation</u>

$$\mathbf{x}(t) = \mathbf{x}(0) + \int_{0}^{t} \dot{\mathbf{x}}(\tau) d\tau$$
$$= \mathbf{x}(0) + t\dot{\mathbf{x}}(0) + \frac{1}{M} \int_{0}^{t} \int_{0}^{\tau} \mathbf{F}(\alpha) d\alpha d\tau,$$

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